Fracture mechanics as an improvement of fatigue life assessment in orthotropic bridge decks

W. Nagy, H. De Backer & Ph. Van Bogaert
Ghent University, Ghent, Belgium

ABSTRACT: Orthotropic bridge decks are widely used in long span steel bridges since they are extremely light weighted when compared with the load carrying capacity. In the past, fatigue life problems have sometimes been overlooked during design. Nowadays, approaches for fatigue design have reached their limits resulting in conservative design leading to overestimating the necessary dimensions. An improved fatigue life assessment method is thus necessary. One possibility is to start using fracture mechanics. These techniques have many advantages since they form a more in-depth analysis. This implies that an entire crack propagation can be evaluated. If the case study of the Temse bridge in Belgium is evaluated, a crack length of 461,703 mm is found while a crack length of 600 mm was detected in reality. Although the results show the effort of fracture mechanics, improvements are still necessary such as implementing residual stresses into the model.

1 INTRODUCTION

Although fatigue in steel constructions is the most important form of fracture, it is the least understood behaviour because of its complexity. In the past, fatigue life problems have sometimes been overlooked during design. Fatigue as a failure mode first came to light in the mid-nineteenth century with Wöhler’s research work in Germany on the premature failure of railroad axles at stresses below the elastic limit (Polák, J. 2003). His work is still used in the form of SN-curves. The problem however is that these curves should be updated for every project where a different design approach or installation procedure is used. Of course, this is mostly not the case leading to a misunderstanding of the fatigue behaviour of the detail being studied. Additionally, the Palmgren-Miner method is used to calculate the lifetime of that detail. The most important advantage of this method is its simplicity while giving a good indication of the remaining lifetime. However, this method is not very accurate because the load history and the load sequences do not have any effect on the fatigue behaviour. These design imperfections lead to overestimating the dimensions when considering orthotropic bridge deck plates.

Orthotropic bridge decks are widely used in long span steel bridges since they are extremely light weighted when compared with the load carrying capacity and are therefore durable and very efficient. These types of bridge decks consist out of a complex network of closed trapezoidal longitudinal stiffeners and transverse web stiffeners welded to a deck plate (Fig. 1).

Because of the latter, various complex welding operations cause multiple fatigue problems across the bridge deck. To investigate the complex fatigue behaviour, other methods are needed besides the traditional way of fatigue calculation. Therefore, a more in-depth analysis is used: fracture mechanics. This method is well known in the aerospace, marine and automobile sector because it can evaluate the crack behaviour in detail. Also a much larger dataset will be available for estimating the total fatigue lifetime or even a more realistic evaluation for the remaining lifetime of existing bridges.

2 DESCRIPTION OF THE PROBLEM

In the past 10 years, several fatigue problems have been observed in several orthotropic bridge decks across Europe. Especially in the Netherlands, where many of
3 CASE STUDY

An example of an orthotropic bridge deck with a poor fatigue behaviour is the Temse bridge across the river Scheldt in Belgium. This bridge is part of an important transport route for heavy lorries to the port of Antwerp.

4 ANALYTICAL STUDY

4.1 General

To verify the fatigue problem in detail, a more sophisticated method is needed instead of the traditional
Figure 6. Large FEM-model of the Temse bridge.

Figure 7. Von Misses stresses of the detailed small-scale model.

SN-curves and the Palmgren-Miner hypothesis as already explained. Therefore, the use of fracture mechanics could give a more detailed and improved look at the problem. To analyse the stiffener-to-deck plate connection detail, a FEM-model was developed in the finite element software Samcef. The advantage of using such software, is the ability to evaluate several fracture mechanics parameters and the crack propagation as well. This is done with an XFEM (eXtended Finite Element Method) method. With this method, the crack growth can be assessed without re-meshing the model in the vicinity of the crack. Although this is a very helpful tool, it needs a huge amount of computation time and power. Especially when the model is complex or when large cracks need to be evaluated.

4.2 FEM-model

In a first stage, a FEM-model is built of the whole movable part of the Temse bridge (Fig. 6). This is done with shell elements and beams. Although this model reflects the real behaviour of the structure well, a more detailed model is needed for studying the fracture mechanics parameters. Therefore, a more detailed small-scale model is constructed consisting of volume elements (Fig. 7).

To relate both models, the displacements and rotations are taken from the first model and introduced on the boundaries of the detailed model. This also implies that the big model is reduced to only the detail being studied, and that the computation time decreases.

4.3 XFEM-model

4.3.1 Manual model

Two possible ways to assess the fatigue life of welded connections with an XFEM-model exist. The first option is to insert a certain number of crack fronts in the weld corresponding to the crack front detected in a damaged detail of a construction. For this case study, an initial elliptical crack of 1 mm (both axes) was inserted at the weld root and perpendicular to the bridge deck (Fig. 9). The choice of this initial crack length could have a great influence on the total fatigue life of the structure. Depending on the welding detail, used construction technologies, lifetime of the structure, etc. an initial crack between 0.1 mm and 1 mm is often chosen (Polák, J. 2003, Nagy, W. et al. 2012). The reason why a 1 mm crack is assumed for this case study relies on a microscopic study of present weld details of a stiffener-to-deck plate connection (De Backer, H. 2006). The difference between several manufacturers is also taken into account.

After the fracture mechanics parameters are gathered from this initial crack, several other crack fronts could be evaluated with incrementing dimensions. An important parameter to evaluate is the stress intensity factor (SIF). This parameter can be used to evaluate the crack growth and its lifetime using one of the many crack propagation laws. In this case, the traditional Paris law is used:

\[
\frac{da}{dN} = C \cdot \Delta K_i^m
\]

where \(C\) and \(m\) are material properties and \(\Delta K_i\) represents the stress intensity factor for mode I cracks. For structural steel \(C = 3.10^{-13} \text{[N, mm]}\) and \(m = 3\) (Maljaars, J. et al. 2012). For the assessment of existing (old) steel bridges, \(C = 4.10^{-13}\) and \(m = 3\) could be used (Kühn, B. et al. 2008).

Knowing the SIF-values for a certain number of crack fronts, it is possible to simulate the geometrical depended parameter \(f(a)\) from equation 2:

\[
\Delta K_i = f(a) \cdot \Delta \sigma \cdot \sqrt{\pi \cdot a}
\]

In this equation \(\Delta \sigma\) represents the applied stress range at the crack front and \(a\) the crack length. The geometrical parameter \(f(a)\) not only depends on the crack length \(a\), but also on the overall dimensions of the bridge deck. Therefore, once this parameter is evaluated for a particular bridge deck geometry and weld detail, this could be used for several other bridges with comparable dimensions.

Finally in order to get more realistic results, the Paris law could be expanded with the threshold value of the SIF-value:

\[
\frac{da}{dN} = C \cdot (\Delta K_i^m - \Delta K_{th}^m)
\]

This threshold value lies between 61 and 80 N/mm\(^{3/2}\) for structural steel (Maljaars, J. et al. 2012, Kühn, B. et al. 2008).
From equation 3 it is now possible to evaluate the total fatigue life of the detail being studied:

\[
N_f = \frac{\sigma}{C \cdot (\Delta K_m^m - \Delta K_m\text{min})}
\]

or:

\[
N_f = \frac{\sigma}{C \cdot ((f(\alpha) \cdot \Delta \sigma \cdot \sqrt{\pi \cdot a})^m - \Delta K_m\text{min})}
\]

### 4.3.2 Automatic model

A second and more accurate option to evaluate the crack front is with an automatic crack propagation method using the full advantage of the XFEM possibilities. Generally, the principle is the same as with the manual method. At first, an initial crack is placed in the model. After that, the XFEM-model uses the Paris law in order to propagate the crack automatically according to the path which uses the least energy to crack:

\[
\frac{da}{dN} = C \cdot (\Delta K_f)^n
\]

The SIF-value in this equation is a function of \(\Delta K_I, \Delta K_{II}, \Delta K_{III}, \theta_p\) (bifurcation angle) and the used material.

Besides the SIF-values and the fatigue lifetime, this method also gives the crack propagation path in a complex three-dimensional way. This is a great advantage in evaluating the weld geometry and their resulting cracks. The only disadvantage of this method is the computational effort. This method only gives accurate results if the mesh is sufficient fine enough around the crack front. Therefore, only relative small cracks could be evaluated with this method.

### 5 RESULTS

Before the XFEM analysis, a FEM analysis is done of the orthotropic bridge deck of the Temse bridge. Figure 7 illustrates the Von Misses stresses in the geometrical detail of the weld, while Figure 8 represents the third principal stresses of a cross section of the detail mid-span two crossbeams.

Figure 8 also indicates a zone of compression at the weld root, which is the location of the initial crack for the XFEM calculation. Therefore, the crack propagation is due to compression and not tension.

According to a traditional fatigue analysis of this bridge deck (De Backer, H. et al. 2006), a total fatigue life of 23.8 years is observed. This incredibly small result indicates that it is obvious that a crack length of 600 mm was detected after 10 years of service life. One of the reasons of this poor result relies on the fact that only a very thin surface layer of 8 mm is used. And as Figure 5 indicates, the deck is already damaged at the crack location in a way that no load dispersion could be possible.

The calculations with the manual XFEM method are done with an initial semi-elliptical crack length of 1 mm as already explained (Fig. 9). In addition, several other cracks with incremented dimensions are evaluated like the larger crack front in Figure 10.

Concerning the applied stresses, model 4 is used conform the Eurocodes (Structural Eurocodes 2010). This implies that a traffic distribution is used with five characteristic lorries. Figure 11 illustrates the location of the corresponding axle loads in relation with the crack location. As a result, Figure 12 and Figure 13 illustrate the SIF-values for all the crack geometries being studied. A best-fit curve could be found representing the formulation for the geometrical parameter \(f(\alpha)\). Therefore, all the SIF-values are known for every crack length and different axle loads. It is also visible
that the crack would propagate much faster in the longitudinal direction and not so fast in the transversal. The crack only propagates much faster transversally, when the crack front counters the tensile zone of Figure 8. This indicates that the crack first propagates longitudinal through the weld before propagating through the deck plate, which confirms the problem of visual inspection of fatigue cracks.

It is known that during the past service live of 10 years, where the crack propagated until the crack length of 600 mm, an approximate load cycle history is equal to:

\[ N = 10\text{years} \cdot 250\text{days} \cdot 2800 \frac{\text{lorries}}{\text{day}} = 7 \cdot 10^6 \]  

(7)

The corresponding fatigue crack with these load cycles could be derived from equation 2 and 3:

\[ a = \sum_i C \cdot (f(a_i) \cdot \Delta \sigma_i \cdot \sqrt{\pi} \cdot a_i)^n - \Delta K_{\Delta}^n \cdot dN \]  

(8)

With this equation, a longitudinal fatigue crack length of 461,703 mm could be found for the 7.10^6 lorries and 10 years of service life. This is smaller than the 600 mm detected in real life, but it must be said that a FEM-model is still an ideal environment with no inhomogeneities. In addition, this model does not take into account any residual stresses, which are most likely present in the weld. Especially because multiple welds intersect at the crack location (Fig. 5) and the welds are not chamfered or treated at the surface to reduce any residual stresses.

5.2 Automatic XFEM-model

As with the manual method, an initial crack length of 1 mm was chosen. Although only a small crack propagation of several mm could be simulated due to the heavy computation time, a clear indication of the crack propagation patch becomes visible. The crack seems to propagate through the weld itself and not through the deck plate. This is not so peculiar because the largest stresses are within the weld throat itself and not in the deck plate (Fig. 8). Why the crack path is different for the crack in real life could be for the same reasons of the manual calculations. Residual stresses have a great influence on the crack initiation stage and also on the crack propagation.

6 CONCLUSIONS

It becomes clear that fracture mechanics as an improvement of the fatigue life assessment in orthotropic bridge decks has many advantages. In the traditional fatigue calculations, there are too many assumptions and simplifications to get accurate results. Especially when different geometries or construction technologies are used. Fracture mechanics on the other hand makes it possible to evaluate every detail separately, this being less conservative. In addition, once a particular detail is properly studied, a geometrical parameter \( f(a) \) imposes itself. Therefore, other similar details could be evaluated without doing an intensive FEM and XFEM calculation.

Application of this method to the case of the Temse bridge in Belgium, resulted in a crack length of 461,703 mm after a service life of 10 years. Compared to the 600 mm of crack length found in reality, this is a good result although a bit optimistic. A possible
explanation is that the model does not take any residual stresses into account. The implementation of such stresses in the model could be an improvement for further research.

REFERENCES


