Characterizing Generated Charged Inverse Micelles with Transient Current Measurements

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ABSTRACT: We investigate the generation of charged inverse micelles in nonpolar surfactant solutions relevant for applications such as electronic ink displays and liquid toners. When a voltage is applied across a thin layer of a nonpolar surfactant solution between planar electrodes, the generation of charged inverse micelles leads to a generation current. From current measurements it appears that such charged inverse micelles generated in the presence of an electric field behave differently compared to those present in equilibrium in the absence of a field. To examine the origin of this difference, transient current measurements in which the applied voltage is suddenly increased are used to measure the mobility and the amount of generated charged inverse micelles. The mobility and the corresponding hydrodynamic size are found to be similar to those of charged inverse micelles present in equilibrium, which indicates that other properties determine their different behavior. The amplitude and shape of the transient currents measured as a function of the surfactant concentration confirm that the charged inverse micelles are generated by bulk disproportionation. A theoretical model based on bulk disproportionation with simulations and analytical approximations is developed to analyze the experimental transient currents.

1. INTRODUCTION

Nonpolar liquids with added surfactant are studied intensively for their relevance in motor oil,† petroleum processing,‡ electrical power transformers,§ electronic ink displays, and liquid toners.¶ In many applications surfactants are used as charging and stabilizing agents for colloidal particles. Since not all added surfactant resides on the particles or at other interfaces, the excess surfactant can form inverse micelles of which a small fraction is charged. These charged inverse micelles are the origin of the often surprisingly high electrical conductivity measured in nonpolar surfactant solutions.¶¶ This conductivity in turn affects the switching behavior if colloidal particles are present.¶¶¶ Measurements based on the pair interaction potential, particle tracking electrophoresis, optical trapping electrophoresis, and blinking tweezers are currently used to probe the electrokinetic properties of nonpolar colloids.¶¶¶ It is observed clearly and can be used to obtain the concentration.
mobility, and hydrodynamic size of the charged inverse micelles. The remaining nonzero current after the transient is related to and limited by the generation of new charged inverse micelles. This generation current can be used to investigate the mechanism and rate with which the charges are generated.\(^{34}\)

In this paper a more detailed investigation of the charge generation process in a nonpolar surfactant system is carried out. We investigate the surfactant polysorbyle succinimide (PIBS) commercially sold as OLOA11K in \(n\)-dodecane. This surfactant is an interesting model system since it has large, slow micelles and a low generation current, and it behaves similar to other surfactants such as Solsperses13940 and SPAN80. Even though many aspects of the generation mechanism of charged inverse micelles in this surfactant system are well-understood, measurements of reversal currents in which the voltage is switched from \(V\) to \(-V\) have revealed a difference between charged inverse micelles present in equilibrium in the absence of an electric field and charged inverse micelles that are newly generated in the presence of a field (unpublished results). In these reversal currents a first maximum occurs which is understood well from drift and diffusion of the initially present charges, but also a second peak is observed that cannot be explained by the existing theoretical model. The second peak is related to newly generated charged inverse micelles since it is absent for short times of the preceding pulse at voltage \(V\) and since it grows (until saturation is reached) if the preceding pulse during which new charges are generated is longer. The fact that the second peak appears at a different time than the expected arrival time of the initially present charges could mean that it is caused by charges with a different mobility. Also, in contrast to the initially present charges, the newly generated charges practically do not contribute to the charge inside the double layer. Altogether, it is clear that newly generated charges behave differently at the electrode surfaces and potentially have a different mobility compared to the initially present charges. Such different behavior could originate from a difference in size or charge-distribution of the inverse micelles. Here, the number and the mobility of newly generated charged inverse micelles is measured using transient current measurements with stepwise increasing voltage (\(V_1 \rightarrow V_2\)). Such information cannot be achieved using just polarizing voltages (\(0 \rightarrow V\)) since this provides only the generation rate of charged inverse micelles but not the mobility or the concentration separately.\(^{34}\) At the same time the amplitude and shape of the measured currents confirm that the newly generated charges are formed by a bulk disproportionation mechanism.

2. THEORY

For the interpretation of transient currents with stepwise increasing voltages (\(V_1 \rightarrow V_2\)) a theoretical model with simulations and analytical formulas is developed in this section. In this model we consider a suspension of inverse micelles placed between two parallel electrodes. We assume that bulk disproportionation (\(2A_0 \leftrightarrow A_+ + A_-\)) is the generation mechanism leading to charged inverse micelles. Then, in equilibrium and in absence of an electric field, the concentration of positively and negatively charged inverse micelles is \(n_+ = n_- = n = (\beta / \alpha) n_0\)\(^{15,11,34,36}\). Here, \(n\) and \(n_0\) are defined as the equilibrium concentrations of charged and uncharged inverse micelles respectively, and \(\beta\) and \(\alpha\) are the generation and recombination rate constants of the disproportionation mechanism. Since the formation of a charged inverse micelle comes at a large free energy cost, we can restrict to the case that \(\beta \ll \alpha\) and therefore that \(n \ll n_0\).\(^{10}\) When a voltage difference is applied across the electrodes, the transient current \(I(t)\) can be modeled with\(^{27,30}\)

\[
I(t) = \sum_i n_i \varepsilon A \frac{\varepsilon s}{d} \int_0^t \Psi_i dx
\]

(1)

Here, \(x\) is the position between the electrodes which are situated at \(x = 0\) and \(x = d\), \(e\) is the elementary charge, \(S\) is the surface area of the electrodes, and \(z_i\) is the valency of micelles where the index \(i\) refers to positive, negative, or neutral inverse micelles. The flux due to drift in the electric field \(E\) and due to diffusion is \(\Psi_i = E n_i \mu_i - D_i (dn_i/dx)\). We will make a distinction between positively and negatively charged micelles which are initially present in equilibrium in absence of an electric field, with concentrations respectively \(n_+\) and \(n_-\) with mobility \(\mu_+ = -\mu_- = \mu\), valency \(z_+ = -z_- = z\), and diffusion coefficient \(D_+ = D_- = D\) and the newly generated positively and negatively charged inverse micelles with concentration respectively \(n_{gen,+}\) and \(n_{gen,-}\) with mobility \(\mu_{gen,+} = -\mu_{gen,-} = \mu_{gen}\), valency \(z_{gen,+} = -z_{gen,-} = z_{gen}\) and \(D_{gen,+} = D_{gen,-} = D_{gen}\). The diffusion coefficient and mobility are related by \(D_i = \mu_i kT/z_i e\) with Boltzmann constant \(k\) and temperature \(T\). Considering the small size of the micelles compared to the Bjerrum length in nonpolar liquids we expect a value \(z = z_{gen} = 1\) for both types of charged inverse micelles.\(^{27,30}\) However, the size and therefore also the mobility and diffusion coefficient of the initially present and newly generated charged inverse micelles can potentially be different. The dynamics of the concentrations are determined by the following continuity equations and Gauss’s law:

\[
\frac{dn_+}{dt} = -\frac{d\Psi_+}{dx}
\]

(2)

\[
\frac{dn_{gen,+}}{dt} = -\frac{d\Psi_{gen,+}}{dx} + \beta n_0^2 - \alpha n_{tot,+} - n_{tot,-}
\]

(3)

\[
\frac{dn_0}{dt} = -\frac{d\Psi_0}{dx} - 2(\beta n_0^2 - \alpha n_{tot,+} n_{tot,-})
\]

(4)

\[
\varepsilon_0 \varepsilon_s \frac{dE}{dx} = \rho
\]

(5)

Here, \(\varepsilon_0\) is the permittivity of vacuum, \(\varepsilon_s\) is the dielectric constant of the liquid, \(t\) is time, and \(\rho = \sum n_i\) is the space charge density conserving overall charge neutrality \(\int_0^d \rho dx = 0\). In the simulations, eqs 1–5 are solved numerically with boundary conditions \(\int_0^d E dx = V_j\) where \(V_j\) is the applied voltage with normalized value \(\phi_j = (zeV_j/kT)\). Blocking conditions for the inverse micelles are assumed at the electrodes: \(\Psi_i (x = 0) = \Psi_i (x = d) = 0\). This is a simplification since we will see in the experiments that at high applied voltages there are additional, but small contributions to the current such as surface generation currents. In eq 2 we assume that the total number \(n dS\) of initially present positively and negatively charged inverse micelles is fixed, hence the absence of generation and recombination terms. In eqs 3 and 4 we assume that the newly generated inverse micelles can also recombine with initially present micelles. Therefore, the recombination term \(\alpha n_{tot,+} n_{tot,-}\) scales with the concentrations \(n_{tot,+} = n_+ + n_{gen,+}\). The neutral inverse micelles with concentration \(n_0\) with diffusion coefficient \(D_0 = D\) but with zero charge and mobility do not contribute to the current.
Next, analytical approximations are derived that offer insight in the measured and simulated transient currents. We restrict to the case of $\eta_1 \gg 1$ such that diffusion in the bulk can be ignored.\textsuperscript{28} The bulk region is defined as the volume between the electrodes excluding the thin double layers with thickness approximately $2d/\eta_1$.\textsuperscript{27} Of course, inside the thin double layers at the electrodes diffusion still plays an important role. We also restrict to low generation rates and high electric fields according to $\alpha \bar{n} \ll \mu_{\text{gen}} V_i/d^2$, which automatically also satisfies $\beta n_0 \ll \mu_{\text{gen}} V_i/d^2$. Since $d^2/\mu_{\text{gen}} V_i$ is the transit time required for generated charges to drift the distance between the electrodes, this means that the field depletes the newly generated charges much faster than they are generated, such that the concentrations of newly generated micelles $n_{\text{gen},+}$ and $n_{\text{gen},-}$ in the bulk are much smaller than the equilibrium concentration $\bar{n}$. As a result the recombination term $-an_{\text{tot},+}n_{\text{tot},-}$ can be ignored in eqs 3 and 4. It also means that the generation of charges is so small that $n_0$ remains roughly equal to the equilibrium value $\bar{n}$ such that $\beta n_0^2$ can be replaced with $\alpha \bar{n}^2$ and the accumulation of newly generated charged inverse micelles at the electrodes is negligible compared to the amount of initially present charges on the time scales considered here.

Let us first consider the system in equilibrium in the absence of a field. If a voltage $V_1$, at $t = 0$ is applied starting from the homogeneous initial situation, we find with eq 5 that the electric field is $E_1 = V_i/d$ and the initial current with eq 1 is $I(0) = 2ze\alpha S\bar{n}V_i/d$. The details of the full transient current related to the initially present charges depend on two parameters: $\eta_1 = zeV_i/\kappa T$ and $\lambda = 2ze^2d^2/\kappa T$, but in all cases where $\eta_1 \gg 1$ the initially present charged inverse micelles eventually get separated\textsuperscript{27,28,30} corresponding to a total transported charge $Q = \kappa T S d$. During this transient the concentration of newly generated inverse micelles gradually increases according to eq 3 until quasi steady-state is reached. In the quasi steady-state situation after the transient, the initially present charged inverse micelles have formed thin double layers at the electrodes with thickness approximately $2d/\eta_1$, and they do not contribute any longer to the electric current. In the case that $\lambda < 20e^2\kappa T$, which is satisfied easily if $\eta_1 \gg 1$, the effect of space-charge in the double layers on the electric field in the bulk is negligible since it is compensated mostly by image-charge in the electrodes.\textsuperscript{27} For example, for $\eta_1 = 394$ and $\lambda = 1.17 \times 10^5$, which corresponds respectively to a typical applied voltage of 10 V and the highest surfactant concentration used in our experiments, the voltage drop over the double layers in steady-state is only about 3% of the applied voltage. As will be confirmed later also the space-charge due to the generated charges in the bulk $ze(n_{\text{gen},+} - n_{\text{gen},-})$ is sufficiently low that its effect on the field can be ignored. Therefore, the field in the bulk is in good approximation $E_1 = V_i/d$. With the above assumptions (ignoring recombination and diffusion), eq 3 can be simplified such that the concentration profile of newly generated charged inverse micelles in the bulk in quasi steady-state is determined by

$$\pm \mu_{\text{gen}} \frac{d n_{\text{gen},\pm}}{dx} = \beta n_0^2$$

(6)

Since no charges are generated at the electrodes, the flux of generated charged inverse micelles is zero at the electrodes of the same polarity, resulting in the boundary condition $\mu_{\text{gen}} E_1 n_{\text{gen},\pm}(x = 0) = \mu_{\text{gen}} E_1 n_{\text{gen},\pm}(x = d) = 0$. Due to the same blocking boundary condition, the newly generated charged inverse micelles accumulate at the oppositely polarized electrodes. However, because of the high applied voltage, these charges are forced into very thin regions at the electrodes where they are almost completely compensated by mirror charges in the electrodes, very similarly as for the initially present charges. As a result the generated charges accumulating at the electrodes have a negligible effect on the steady-state situation at voltage $V_1$, as well as on the transient current upon increasing the voltage from $V_1$ to $V_2$. In our analytical model we have approximated this situation by ignoring diffusion which even results in infinitely thin layers of accumulating charge at the electrodes and consequently full neutralization by mirror charges. Therefore, if we ignore these thin, electrically neutralized layers of charge at the attracting electrodes, the concentration profile of generated charges in the bulk can be described mathematically by not applying the blocking boundary condition at the attracting electrodes.\textsuperscript{28} Then, eq 6 is also valid at the electrode of opposite polarity to the micelle charge. With these boundary conditions eq 6 results in linearly increasing and decreasing concentration profiles of positively and negatively charged newly generated inverse micelles: $n_{\text{gen},+} = \beta n_0^2 dS/\mu_{\text{gen}} V_i$ and $n_{\text{gen},-} = \beta n_0^2 (1 - (x/d))/\mu_{\text{gen}} V_i$. As expected, the flux of generated charged inverse micelles is then zero at the electrode of the same polarity while the maximum flux is $\beta n_0^2 dS/\mu_{\text{gen}} V_i$ at the oppositely polarized electrode. Then, the number of generated positively (or negatively) charged micelles in the bulk is $N_{\text{gen},+} = (\beta n_0^2 dS/2\mu_{\text{gen}} V_i)$ corresponding to an average concentration of $n_{\text{gen},+} = (\beta n_0^2 dS/2\mu_{\text{gen}} V_i)$. The fact that the concentration of generated charges in the bulk scales inversely with voltage is counterintuitive. It can be understood from the fact that the generation rate is independent of the voltage. Therefore, a higher electric field does not generate more charges but in contrast depletes the charges faster and reduces their concentration. We can now re-evaluate the assumption of low space-charge in the bulk. From eq 5 it can be shown that by assuming $(ze\beta n_0^2 dS/\kappa T) \ll V_i^2$ the field in the bulk is not affected by the space-charge due to the generated charges, such that the assumption of a bulk field $E_1 = V_i/d$ is valid. The nonzero quasi steady-state current $I_{\text{gen,lim}}$ is obtained from eq 1:

$$I_{\text{gen,lim}} = \frac{2ze \beta n_0^2 dS}{2\mu_{\text{gen}} V_i} \left( \frac{N_{\text{gen},+}}{d^2} \right) = \beta n_0^2 ze dS$$

(7)

Equation 7 illustrates why $I_{\text{gen,lim}}$ does not depend on the applied voltage or the mobility $\mu_{\text{gen}}$ of the newly generated charged inverse micelles. The first factor between brackets $(2ze(\beta n_0^2 dS/2\mu_{\text{gen}} V_i))$ is the total charge $2zeN_{\text{gen},+}$ of generated charged inverse micelles in the bulk, which decreases with the speed $\mu_{\text{gen}} V_i/d$ of the micelles. The second factor $(\mu_{\text{gen}} V_i/d^2)$ however increases proportionally with this speed. This factor is the inverse of the transit-time for generated charged inverse micelles moving with speed $\mu_{\text{gen}} V_i/d$. Therefore, both $\mu_{\text{gen}}$ and $V_i$ disappear from the formula, and $I_{\text{gen,lim}}$ is called the “generation-limited” current. It is also called a “quasi steady-state” current since on a much longer time scale the bulk concentration of uncharged micelles will eventually decrease and the charge at the electrodes will increase by the continuous generation.

When, in the quasi steady-state situation at applied voltage $V_1$, the voltage is switched to a higher voltage ($V_1 \rightarrow V_2$) at $t = 0$, the resulting current can be interpreted as the sum of two parts: the transient generation current $I_{\text{gen,trans}}(t)$ due to
generated charged inverse micelles and the double layer rearrangement current $I_{DL}(t)$ related to the initially present charged inverse micelles:

$$I_{\text{gen}}(t) = I_{\text{gen,trans}}(t) + I_{\text{DL}}(t)$$  \hfill (8)

The transient generation current $I_{\text{gen,trans}}(t)$ has two contributions. One is related to the fixed amount of generated charged inverse micelles $N_{\text{gen}}$ already present at $t = 0$ which suddenly move faster due to the increased field, while another contribution results from newly generated charged inverse micelles. The concentration profile $n_{\text{gen,x}}$ related to the fixed amount of charge of the first contribution can be modeled according to eq 3 but without the generation and recombination term and ignoring diffusion:

$$\frac{dn_{\text{gen,x}}}{dt} = \frac{d}{dx} n_{\text{gen,x}}$$  \hfill (9)

Here, the field in the bulk is given by $E_x = V/d$. Using the steady-state concentration of generated charged micelles in the bulk given by eq 6, we find that the gradient $(dn_{\text{gen,x}}/dx) = \frac{1}{\mu_0 V_2} (\beta n_{\text{gen}}(x)/\mu_0 V_2)$ at $t = 0$ is independent of the position. Therefore, eq 9 results in $(dn_{\text{gen,x}}/dt) = -(V_2/V_1) n_0^2$, showing that the concentration at each position $x$ decreases linearly in time at the same rate until it reaches the new equilibrium value $n_{\text{gen,eq}} = \beta n_0^2 dx/\mu_0 V_2$ and $n_{\text{gen,eq}} = \beta n_0^2 d(1 - (x/d))/\mu_0 V_2$. Two regions are formed as time passes, one in which the new equilibrium is already reached, and one in which the gradient remains $(dn_{\text{gen,x}}/dx) = \frac{1}{\mu_0 V_2} (\beta n_0^2/\mu_0 V_2)$. The resulting concentration $n_{\text{gen,x}}(x, t)$ during the transient is given by

$$n_{\text{gen,x}} = \begin{cases} \frac{\beta n_0^2 d}{\mu_0 V_2} & x \in \left[0, \frac{\mu_0 V_2 t}{d}\right] \\ \frac{\beta n_0^2 d}{\mu_0 V_1} - \frac{\beta n_0^2 d}{\mu_0 V_1} (\frac{V_2}{V_1} - 1) & x \in \left[\frac{\mu_0 V_2 t}{d}, d\right] \end{cases}$$  \hfill (10)

where $n_{\text{gen,eq}}(x) = n_{\text{gen,eq}}(d - x, t)$. With eq 1 while ignoring diffusion by using $V_x = \mu_0 \mu$, the corresponding transient generation current becomes

$$I_{\text{gen,trans}}(t) = \left\{ \begin{array}{ll} \mu_0^2 \beta n_{\text{zed}} \left[ \frac{2}{V_1} \left( \frac{V_1}{V_2} - 1 \right) \right] & 0 \leq t \leq \frac{\mu_0}{\beta n_{\text{zed}}} \frac{d}{V_2} \left( \frac{V_2}{V_1} - 1 \right) \\ \mu_0^2 \beta n_{\text{zed}} S \Delta t & t > \frac{\mu_0}{\beta n_{\text{zed}}} \frac{d}{V_2} \left( \frac{V_2}{V_1} - 1 \right) \end{array} \right\}$$  \hfill (11)

The initial current $I_{\text{gen,trans}}(0) = V_2/V_1 \times I_{\text{gen,lim}}$ is again independent of the mobility of the generated micelles. But the transit time $t_{\text{trans}} = (d^2/\mu_0 V_2)$ for the generated micelles to reach the electrodes in the field $V_2/d$ or for the current to return to the generation-limited value does depend on $\mu_0$. $I_{\text{gen,trans}}(t)$ is a quadratically decreasing current with time. Considering the derivative of the current at $t = 0$, initially the current appears to be linearly decreasing and would become zero at $t = (t_{\text{trans}})^2/(V_2/V_1 - V_1)$, but at this time the actual current is $I_{\text{gen,trans}}(t = (t_{\text{trans}})^2/(V_2/V_1 - V_1)) = I_{\text{gen,trans}}(t = 0) \times (V_2/V_1 - V_1)$. For values of $V_2/V_1 \gg 1$, this means that $I_{\text{gen,trans}}(t)$ first decreases in the time $t_{\text{trans}}$ to a quarter of the initial value, followed by a three times slower decrease until the current reaches steady-state at $t = t_{\text{trans}}$. After the transient the remaining quasi steady-state current $I_{\text{gen,lim}}$ causes an additional transported charge $\mu_0^2 \beta n_{\text{zed}} S \Delta t$ in each time interval $\Delta t$.

A charge moving between the electrodes causes a continuous current in the external circuit until it reaches the attracting electrode. The integral of the current is therefore a measure of the number of charges in the bulk and the amount of time they travel toward the electrodes. Equation 12 shows the integral of the transient generation current in eq 11 from $t = 0$ to $t = t_{\text{trans}}$, which corresponds to the charge transported from the bulk toward the electrodes in the transit time. This charge can be written as the sum of two contributions. The first part due to the initially present generated charges is inversely proportional to the voltage $V_1$, since the concentration of generated charged inverse micelles is reduced for increasing $V_1$. The second part is due to the generation of new charged inverse micelles, and this is inversely proportional to $V_2$. 

Figure 1. Simulation (black line), analytical model for the transient generation current (red line), level of the generation-limited current (dotted red line), and transient current measurement (blue dots) in (a) for $n = 439 \ \mu m^{-3}$, $V_1 = 30 \ V$, and $V_2 = 60 \ V$ and in (b) for $n = 70 \ \mu m^{-3}$, $V_1 = 3 \ V$, and $V_2 = 10 \ V$. In (c–d), the corresponding concentration profiles of positive (red lines) and negative (blue lines) charges are shown at linearly spaced times during the transient.
\[
Q_{\text{gen,trans}} = \frac{\beta n_0^2 z e S d^3}{3 \eta_{\text{gen}_1} V_1} + \frac{2 \beta n_0^2 z e S d^3}{3 \eta_{\text{gen}_2} V_2}
\]

(12)

For large values of \(V_2 / V_1\), \(Q_{\text{gen,trans}}\) becomes almost equal to \(2 \pi \alpha^2 \eta_{\text{gen},z} / \beta \) such that the measurement of \(Q_{\text{gen,trans}}\) can be used to estimate \(\eta_{\text{gen},z}\). The mobility \(\mu_{\text{gen}}\) can be estimated from the transit time \(t_{\text{gen}} = (d^2 / \mu_{\text{gen}} V_2)\) or using \(Q_{\text{gen,trans}} = \eta_{\text{gen},z}(V_2)\). (\(t_{\text{gen}} / 3\)). The parabolic shape of the transient current is a direct result of the assumption of bulk generation, since in the steady-state this leads to a linearly increasing or decreasing concentrations of generated charges between the electrodes. In contrast, surface generation would lead to a uniform distribution of generated charged micelles, and to a linearly decreasing transient generation current with the same transit time \(t_{\text{gen}} = (d^2 / \mu_{\text{gen}} V_2)\). Therefore, analysis of the measured transient generation current not only provides \(\mu_{\text{gen}}\) and \(\eta_{\text{gen},z}\) it can also confirm bulk generation as the origin of the generation current.

The second part in eq 8, the double-layer current \(I_{\text{DL}}(t)\), is the result of the rearrangement of the double-layers of the initially present positively and negatively charged inverse micelles, both having a fixed total charge \(\pm S\). In the steady-state at voltage \(V_1\), the electric field is roughly \(E \cong V_1 / d\) in the bulk, but close to the electrodes the field increases strongly. Inside the thin double-layers at the electrodes the drift caused by the electric field is compensated by diffusion, such that these charges have a zero current contribution. When at \(t = 0\) the voltage is increased to \(V_2\), the charge \(\pm S\) in both the positively and negatively charged double layer experiences an additional field \(E = (V_2 - V_1) / d\) which is not compensated by diffusion. The net particle flux in the double layers becomes \(\Psi_{\pm} = \pm \mu_{\text{gen}} (V_2 - V_1) / d\) causing the concentration distributions to shift toward the attracting electrodes with speed \(v = \mu (V_2 - V_1) / d\). The corresponding current at \(t = 0\) is straightforward: \(I_{\text{DL}}(0) = 2 \pi e \mu_{\text{gen}} (V_2 - V_1) / d\). The current decreases rapidly at time scales \(t < 2 d^2 / (\mu (V_2 - V_1))\) which is roughly the time needed for the nonlinear part of the double layer to reach equilibrium. After that, the linear part of the double layer reaches the new equilibrium leading to an exponentially decreasing current with amplitude \(8 \pi e n_{\text{gen}} \mu_{\text{gen}} (\Psi_{\pm} / \lambda) (V_2 - V_1) / d\) and time constant \(\tau = d^2 / (\mu e_0 \mu_{\text{gen}})\) (see Supporting Information):

\[
I_{\text{DL,linear}}(t) \cong 8 \pi e n_{\text{gen}} \Psi_{\pm} \frac{V_2 - V_1}{d} e^{-t/\tau}
\]

(13)

Figure 1 illustrates both the numerical simulation model and the analytical equations described above. In these simulations eqs 2–5 are solved with the appropriate boundary conditions and with parameters matching with some of the experiments (see Section 3). More precisely, Figures 1a and c correspond to measurements with mass fraction \(\phi_m = 0.01\) of OLOA11K in dodecane, using simulation parameters \(S = 10^{-14} m^2, d = 19.5 \mu m, e = 2, T = 298 K, n = 439 \mu m^3, \mu = \mu_{\text{gen}} = 1.00 \times 10^{-9} m^2 V^{-1} s^{-1}, \alpha = 5.1 \times 10^{-22} m^3 s^{-1}, V_1 = 30 V, \) and \(V_2 = 60 V\). Figures 1b and d correspond to measurements of \(\phi_m = 0.01\) with the same parameters except \(n = 70 \mu m^3, \mu = \mu_{\text{gen}} = 1.15 \times 10^{-9} m^2 V^{-1} s^{-1}, \) \(\alpha = 2.05 \times 10^{-22} m^3 s^{-1}, V_1 = 3 V, \) and \(V_2 = 10 V\). Using the value \((\alpha / \beta)^{1/2} \cong 1\) estimated from the very similar surfactant OLOA1200, corresponding values for \(\beta\) and \(\eta_{\text{gen}}\) are obtained. Since \(\beta \ll \alpha\) the generation rate is in good approximation \(\beta n_0 \cong \alpha n_0\). In Figure 1a and b, the simulated electric current (black line) is shown, together with the analytical formula for the transient generation current in eq 11 (red line) and the level of the generation-limited current (dotted red line). Also measurements are shown corresponding to these parameters (blue dots) which are discussed in more detail in Section 3. The initial current \(I_0 = I_{\text{DL}}(0)\) in the simulations matches well with the formula of the double layer current \(I_{\text{DL}}(0) = 2 \pi e \mu_{\text{gen}} (V_2 - V_1) / d\). As explained earlier, the current decreases rapidly at time scales \(t < 2 d^2 / (\mu (V_2 - V_1))\) due to the nonlinear part of the double layer reaching its new equilibrium. This time scale corresponds to \(t < 21 \mu s\) in Figure 1a and \(t < 0.9 m s\) in Figure 1b. After that the double layer current decreases roughly exponentially due to the linear part of the double layer reaching equilibrium, matching well in amplitude and time-scale with the exponential decay given in eq 13. However, this exponential part of the double layer current cannot be observed in the total current because of the larger contribution from the transient generation current at \(t > 40 \mu s\) in Figure 1a and \(t > 1 m s\) in Figure 1b. After that time the simulated current matches well with the analytical model of the transient generation current (eq 11). Figure 1c and d give the concentrations of positive charges (red) and negative charges (blue) at times \(t = j \times 2 d^2 / (\mu e_0 \mu_{\text{gen}})\) with \(j = 0, 1, \ldots, 10\). The linearly decreasing concentration profile with time given by eq 10 is illustrated in Figure 1c. When the voltage \(V_1\) is not sufficiently high, the space-charge due to the generated charged inverse micelles can lead to a steady-state bulk field that is lower than \(E \cong V_1 / d\) and spatially inhomogeneous. As a result of \(E < V_1 / d\), the concentration of generated charges in steady-state can be higher than expected from eq 10 and nonlinearly increasing. This case is illustrated in Figure 1d, where the curve for \(t = 0\) corresponds to the steady-state distribution at voltage \(V_1\). As a result the simulated transient generation current shown in Figure 1b is slightly higher than predicted by the model.

3. TRANSIENT CURRENT EXPERIMENTS

3.1. Materials and Methods. Solutions are prepared with mass fractions \(\phi_m = 0.01, 0.03,\) and 0.1 of OLOA11K (Chevron Orontite) in n-dodecane (Rectapur, WVR). The solutions are inserted in a device with plane parallel, plain ITO electrodes with overlapping area \(S = 10^{-4} m^2\). The two electrodes are separated at fixed at a certain distance using UV-curing glue (Norland Optics) containing spacer beads. The distance \(d = 19.5 \mu m\) is measured with interferometry (PerkinElmer Lambda 950). The current measurements are performed using a custom-built setup consisting of a Keithley 428 current amplifier and a National Instruments USB-6212 data acquisition module for the synchronized generation of voltages and the sampling of the electric current. The cell is placed inside a closed metallic box to screen it from external electric fields and is measured at room temperature. To obtain homogenous initial conditions, the electrodes are short-circuited for 500 s before each measurement. Currents measured for pure dodecane (\(\phi_m = 0\)) are roughly 500 times lower than those for the lowest surfactant concentration used here and are limited by the sensitivity of the experimental setup. This corresponds to a bulk conductivity of dodecane below \(10^{-15} \Omega^{-1} m^{-1}\), indicating that the used dodecane does not contain much charge contaminants.

3.2. Measurements. Transient currents have been measured for the different concentrations of OLOA11K and for different applied voltage steps across the electrodes: 0 V \(\rightarrow V_1\) (polarizing current) and \(V_1 \rightarrow V_2\) (transient generation
The polarizing voltages are applied for 40 s, which is sufficient to completely separate the initially present charges. Figure 2 shows the results for the currents for \( V_1 \rightarrow V_2 \), in (a) for \( \phi_m = 0.01 \) and in (b) for \( \phi_m = 0.03 \), both with \( V_1 = 3 \) V and \( V_2 = 6, 10, 20, 30, 40, 50, \) and 60 V, and in (c) for \( \phi_m = 0.1 \) with \( V_1 = 10 \) V and \( V_2 = 20, 30, 40, 60, 80, \) and 100 V. For each experiment four measurement runs are averaged.

**3.3. Analysis.** Using the theory from Section 2, we can now analyze the transient currents in more detail. From the polarizing currents (0 V \( \rightarrow \) \( V_1 \)) (not shown) the equilibrium concentration of initially present charged inverse micelles can be estimated as \( \bar{n} = \int_0^\infty (I(t) - I_{ss}) \, dt / \varepsilon_0 \), where \( I_{ss} \) is the small quasi steady-state current obtained at \( t = 10 \) s and \( t_p \) is the transit time at which all initially present charges have arrived at the electrodes. Figure 3 shows that the obtained concentrations \( \bar{n} = 70, 165, \) and 439 \( \mu m^3 \), respectively, for \( \phi_m = 0.01, 0.03, \) and 0.1 follow roughly the linear relation \( \bar{n} \approx 4500 \, \mu m^3 \times \phi_m \) (red trendline) which is in good agreement with values for OLOA1200.\(^{27,31,34}\) As explained in Section 2, from the law of mass action for disproportionation it is expected that \( \bar{n} \) is proportional to \( n_0 \). If we assume that the concentration of inverse micelles scales proportionally to the surfactant concentration, this leads to a proportionality between \( \bar{n} \) and \( \phi_m \). Therefore, the observed proportionality between \( \bar{n} \) and \( \phi_m \) validates the assumption of a disproportionation generation mechanism.

The mobility of the initially present charges is obtained as \( \mu = I(0) / d / 2 \varepsilon_0 \varepsilon_S V_1 \). The diffusion coefficient \( D = \mu kT / \varepsilon_0 \) is used to obtain the hydrodynamic radius of the charged inverse micelles \( r_z = kT / 6 \pi \eta D \) with the viscosity of dodecane \( \eta = 1.38 \times 10^{-3} \) Pa.s. For the mobilities we find \( \mu = 1.15 \times 10^{-9} \, m^2 \, V^{-1} \, s^{-1} \), \( 1.25 \times 10^{-9} \, m^2 \, V^{-1} \, s^{-1} \), and \( 1.00 \times 10^{-9} \, m^2 \, V^{-1} \, s^{-1} \), respectively, for \( \phi_m = 0.01, 0.03, \) and 0.1, so \( \mu \approx (1.1 \pm 0.1) \times 10^{-9} \, m^2 \, V^{-1} \, s^{-1} \), \( D \approx (2.9 \pm 0.2) \times 10^{-11} \, m^2 \, s^{-1} \), and \( r_z = (5.5 \pm 0.7) \) nm. This size of the inverse micelles is consistent with previous studies with transient current measurements showing a radius of about 6–7 nm.\(^{22,27,31}\)

In Figure 2, it can be observed that the quasi-steady-state current increases slightly (less than a factor 1.5) when the voltage increases a factor of 10 (from 6 to 60 V) or a factor of 5 (from 20 to 100 V), which is not expected in our model of bulk disproportionation leading to a voltage-independent, generation-limited current. The observed increase in current can be attributed to small additional effects such as surface generation which will be ignored in our analysis. Figure 4 shows the generation-limited currents \( I_{gen,lim} = 3.14 \times 10^{-10} \) A, \( 2.5 \times 10^{-9} \) A, and \( 3.05 \times 10^{-8} \) A, respectively, for \( \phi_m = 0.01, 0.03, \) and 0.1, obtained at 6 V for \( \phi_m = 0.01 \) and 0.03 and at 20 V for \( \phi_m = 0.1 \). Using \( I_{gen,lim} = \beta n_0 \bar{v}_d \) from eq 7, this allows us to obtain \( \beta = \bar{v}_d \) from an estimation of the concentration of uncharged inverse micelles in OLOA1200.\(^{29,35}\) Considering the linear relationship between \( \bar{n} \) and \( \phi_m \) (see Figure 3) the trendline \( I_{gen,lim} = 3.05 \times 10^{-6} \) A \( \times \phi_m \) shows that \( I_{gen,lim} \) is in fact proportional to \( \bar{n}^2 \), which is expected for a disproportionation model. The average value of the recombination constant is \( \alpha = 3.4 \times 10^{-22} \, m^3 \, s^{-1} \).

Using the analytical model and simulations, we can now extract the concentration and mobility of newly generated
charged inverse micelles from the transient generation currents in Figure 2a–c. An estimation of \(Q_{\text{gen,trans}}\) can be made by integrating the current while correcting for the exponential part of the double layer current and the quasi steady-state current. In a first example of the measurement in Figure 2b with \(\phi_m = 0.03\), \(V_1 = 3\ \text{V}\) and \(V_2 = 60\ \text{V}\), we find \(Q_{\text{gen,trans}} = 1.51 \times 10^{-10}\ \text{C}\). Then, under the assumption that \(Q_{\text{gen,trans}} = 2\epsilon n_{\text{gen,z}}/3\), which is valid for large values of \(V_f/V_1\), the value \(n_{\text{gen,z}} = 1.41 \times 10^2\) is obtained for the amount of generated charged inverse micelles present in the bulk in steady state at voltage \(V_1 = 3\ \text{V}\). This corresponds to an average concentration of \((n_{\text{gen,z}}) = 0.72 \mu\text{m}^{-3}\), which is 230 times lower than the equilibrium concentration \(\bar{n} = 165 \mu\text{m}^{-3}\). The transit time \(t_{t,2} = 5.1\ \text{ms}\) can be used to estimate the mobility of the newly generated charged inverse micelles \(\mu_{\text{gen}} = d^2/t_{t,2} V_2 = 1.24 \times 10^{-3}\ \text{m}^2\ \text{V}^{-1}\ \text{s}^{-1}\). This mobility corresponds well with the value \(\mu = 1.25 \times 10^{-9}\ \text{m}^2\ \text{V}^{-1}\ \text{s}^{-1}\) of the initially present charged inverse micelles obtained for \(\phi_m = 0.03\). In a second example of the measurement in Figure 2c with \(\phi_m = 0.1\), \(V_1 = 10\ \text{V}\) and \(V_2 = 60\ \text{V}\), we find \(Q_{\text{gen,trans}} = 4.16 \times 10^{-10}\ \text{C}\) with corresponding values \(n_{\text{gen,z}} = 3.90 \times 10^2\) and \((n_{\text{gen,z}}) = 2.00 \mu\text{m}^{-3}\) (220 times lower than the equilibrium concentration \(n = 439 \mu\text{m}^{-3}\)). The transit time \(t_{t,2} = 5.3\ \text{ms}\) results in \(\mu_{\text{gen}} = 1.20 \times 10^{-7}\ \text{m}^2\ \text{V}^{-1}\ \text{s}^{-1}\), which is comparable to the value \(\mu = 1.00 \times 10^{-7}\ \text{m}^2\ \text{V}^{-1}\ \text{s}^{-1}\) of the initially present charged inverse micelles obtained for \(\phi_m = 0.1\).

A good agreement is obtained between the simulations and the experiments of Figure 2 taking values of \(\mu_{\text{gen}}\) that are equal to \(\mu\). Therefore, we can assume that the size of newly generated inverse micelles is about the same as the size of the initially present charged inverse micelles. The simulations in Figure 2 are carried out with parameters \(S = 10^{-4}\ \text{m}^2\ \text{d} = 19.5\ \mu\text{m}\), \(e = 2\), and \(T = 298\ \text{K}\) and in (a) for \(n = 70\ \mu\text{m}^{-3}\), \(\mu = \mu_{\text{gen}} = 1.15 \times 10^{-9}\ \text{m}^2\ \text{V}^{-1}\ \text{s}^{-1}\), \(\alpha = 2.05 \times 10^{-22}\ \text{m}^3\ \text{s}^{-1}\), in (b) for \(n = 165\ \mu\text{m}^{-3}\), \(\mu = \mu_{\text{gen}} = 1.25 \times 10^{-9}\ \text{m}^2\ \text{V}^{-1}\ \text{s}^{-1}\), \(\alpha = 2.94 \times 10^{-22}\ \text{m}^3\ \text{s}^{-1}\), and in (c) for \(n = 439\ \mu\text{m}^{-3}\), \(\mu = \mu_{\text{gen}} = 1.00 \times 10^{-9}\ \text{m}^2\ \text{V}^{-1}\ \text{s}^{-1}\), \(\alpha = 5.1 \times 10^{-22}\ \text{m}^3\ \text{s}^{-1}\) for \(V_1 = 10\ \text{V}\) and \(V_2 = 20, 30, 40, 60, 80, 100\ \text{V}\).

Figure 5 shows data from Figure 2c on a linear scale, illustrating that the transient generation current can indeed be described well by the quadratically decreasing current in eq 11. For better visibility, the time axis has been normalized to the transit-time \(t_{t,2} = (d^2/\mu_{\text{gen},V_2})\), using fixed values \(d = 19.5\ \mu\text{m}\) and \(\mu_{\text{gen}} = 1.15 \times 10^{-9}\ \text{m}^2\ \text{V}^{-1}\ \text{s}^{-1}\). This provides direct evidence for a bulk generation mechanism. For comparison, if surface generation was the mechanism generating the charges, there would be a homogeneous concentration of charges in steady state, and the transient generation current would be linearly decreasing. Fitting a linearly decreasing current to the experimental data would result in two times higher values of the mobility as for the case of bulk generation. However, surface generation is in contradiction with the observation that the generation-limited current is proportional to \(d\) (for OLOA1200\textsuperscript{27,34}), which indicates that the generation is occurring in the bulk. While there is a good match between measurement and simulation for \(V_2 > 30\ \text{V}\) in Figure 2b and c, it should be noted that for \(V_2 > 30\ \text{V}\) an additional linearly decreasing current appears corresponding to charges with a higher mobility. The fact that this effect is absent for low values of \(V_2\) but becomes more important for higher voltages \(V_2\) suggests that these faster charges are released from the electrodes when increasing the voltage to \(V_2\) rather than that they are already present in the bulk in steady-state.

Since the part of the double layer current before \(t = 10^{-4}\ \text{s}\) cannot be measured with our setup, \(Q_{\text{DL}}\) cannot be estimated. Only between \(t = 10^{-4}\ \text{s}\) and \(t = 10^{-3}\ \text{s}\) in the different measurements of Figure 2, the good agreement in both amplitude and time-scale can be observed between measurements and simulations of the double layer current. This confirms that in steady-state the initially present charged inverse micelles form a diffuse double layer as expected from the Nernst–Planck–Poisson equations.

4. DISCUSSION

The described transient generation current method is applicable with some restrictions. The generation rate of the surfactant system should be sufficiently low and the voltage \(V_1\) high enough such that the generation-limited steady-state current can be measured. But \(V_2/V_1\) should also be large enough to get a sufficiently high amplitude of the transient generation current. However, the higher \(V_2\) the faster this transient occurs, and the more difficult it becomes to measure. Since the generation-limited current scales quadratically with \(\phi_m\) for \(\phi_m \ll 0.1\) the generation-limited current becomes so low that the measurement sensitivity and other current generation effects start playing a role. For that reason it is difficult to draw conclusions from the data from Figure 1a other than that the time-constants and amplitudes are roughly as expected. For concentrations \(0.01 < \phi_m < 0.1\), the signal-to-noise ratio is good. For high concentrations \((\phi_m \gg 0.1)\), the generation rate increases, and higher voltages are required to measure the generation-limited current. Also, the presented theory and analytical model should be modified depending on the electrical behavior of the surfactant solution. For example, for AOT in dodecane the double layer current will be absent since the charged AOT inverse micelles do not form a classical double layer.\textsuperscript{15,32,33}

The presented results confirm in more detail the established theory that bulk disproportionation is the dominant generation mechanism at typical surfactant concentrations. However, the knowledge that a similar hydrodynamic size is obtained for both the newly generated and the initially present charged inverse micelles is an important step toward understanding the differences which have been observed between both types of micelles.
5. CONCLUSION

In conclusion, the analysis of transient generation currents with stepwise increasing voltages has been used to investigate the generation mechanism of charged inverse micelles of the surfactant OLOA11K in dodecane. Simulations and analytical approximations based on bulk disproportionation have been developed to analyze the current measurements. It is found that the size of the newly generated charged inverse micelles is roughly the same as the size of the charged inverse micelles present in equilibrium, which is important in understanding observed differences between both types of micelles. A detailed current analysis confirms that the charges are generated in the bulk and according to a disproportionation mechanism.

■ ASSOCIATED CONTENT

Supporting Information
Analytical model for the double layer current. This material is available free of charge via the Internet at http://pubs.acs.org.

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